

THE UNIVERSITY OF BRITISH COLUMBIA

## Physics 108 Assignment # 9: INDUCTANCE & CIRCUITS

Wed. 9 Mar. 2005 — finish by Wed. 16 Mar.

1. **Solenoid as an  $RL$  Circuit:** A long wire with net resistance  $R = 120 \Omega$  is wound onto a nonmagnetic spindle to make a solenoid whose cross-sectional area is  $A = 0.02 \text{ m}^2$  and whose effective length is  $\ell = 0.5 \text{ m}$ . (Treat the coil as an ideal, long solenoid.) Using a battery with a  $1 \text{ M}\Omega$  internal resistance, a magnetic field of  $B_0 = 0.6 \text{ T}$  has been built up inside the solenoid. At  $t = 0$  the battery is shorted out and then disconnected so that the current begins to be dissipated by the coil's resistance  $R$ . We find that after  $3.6 \text{ ms}$  the field in the coil has fallen to  $0.1 \text{ T}$ .
  - (a) How many joules of energy are stored in the coil at  $t = 0$ ?
  - (b) How long does it take for the stored energy to fall to half its initial value?
  - (c) What is the total number of turns in the coil?
2.  **$LC$  Circuit Time-Dependence:** In an  $LC$  circuit with  $C = 90 \mu\text{F}$  the current is given as a function of time by  $I = 3.4 \cos(1800t + 1.25)$ , where  $t$  is in seconds and  $I$  is in amperes.
  - (a) How soon after  $t = 0$  will the current reach its maximum value?
  - (b) Calculate the inductance.
  - (c) Find the total energy in the circuit.
3. **Build Your Own Circuit:** You are given a  $12 \text{ mH}$  inductor and two capacitors of  $7.0$  and  $3.0 \mu\text{F}$  capacitance. List all the resonant frequencies that can be produced by connecting these circuit elements in various combinations.
4.  **$LRR$  Circuit Time-Dependence:** In the circuit shown, the  $\mathcal{E} = 12 \text{ V}$  battery has negligible internal resistance, the inductance of the coil is  $L = 0.12 \text{ H}$  and the resistances are  $R_1 = 120 \Omega$  and  $R_2 = 70 \Omega$ . The switch **S** is closed for several seconds, then opened. Make a quantitatively labelled graph with an abscissa of time (in milliseconds) showing the potential of point **A** with respect to ground, just before and then for  $10 \text{ ms}$  after the opening of the switch. Show also the variation of the potential at point **B** over the same time period.

