

NUCLEAR PHYSICS

an

Introduction

by

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Conversion of Mass to Energy

Einstein's association of the term mc^2 with a **rest mass energy** E_0 naturally led to speculation about what might be done to *convert* mass into useable energy, since for a *little* mass you get a *lot* of energy!

Let's see *just how much*: in *S.I.* units $1 \text{ J} \equiv 1 \text{ kg}\cdot\text{m}^2/\text{s}^2$ so a 1 kg mass has a rest mass energy of $(1 \text{ kg}) \times (2.9979 \times 10^8 \text{ m/s})^2 = 8.9876 \times 10^{16} \text{ J}$ — which is a lot of joules! To get an idea how many, remember that one **watt** is a unit of *power* equal to one joule per second, so a **joule** is the same thing as a **watt-second**. Therefore a device converting *one millionth of a gram* ($1 \mu\text{g}$) of mass to energy *every second* would release approximately *90 megawatts* [millions of watts] of power!

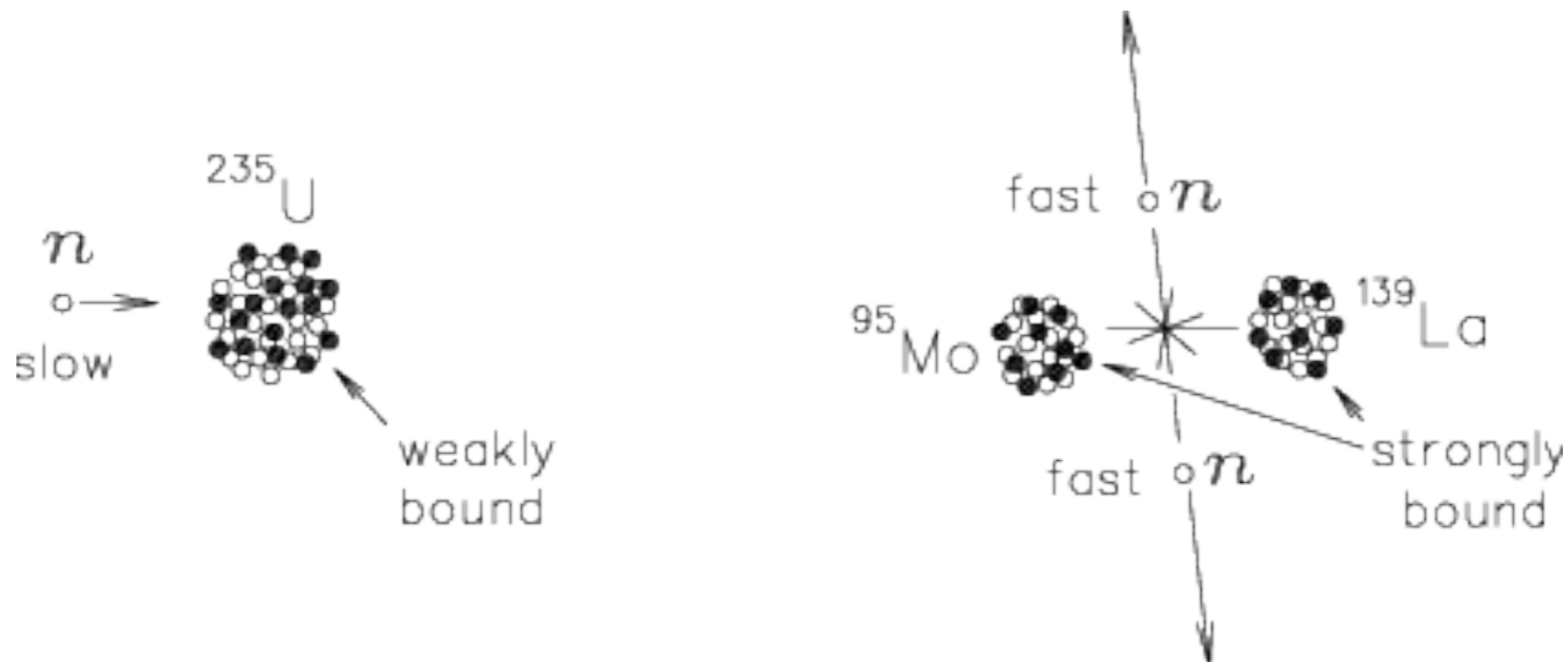
Bad Things to do with Mass-Energy Conversion

Contrary to popular belief, the first conclusive demonstration of mass-energy conversion was in a controlled nuclear *reactor*.

However, not long after came the more unpleasant manifestation of mass-energy conversion: the fission *bomb*. An unpleasant subject, but one about which it behooves us to be knowledgeable. For this, we need a new energy unit, namely the **kiloton** [kt], referring to the energy released in the explosion of one thousand *tons* of TNT [*TriNitroToluene*], a common chemical high explosive. The basic conversion factor is $1 \text{ kt} \equiv 1 \text{ trillion calories} = 4.186 \times 10^{12} \text{ J}$, which means that one **kiloton**'s worth of energy is released in the conversion of 0.04658 grams [46.58 mg] of mass. Thus a **megaton** [equivalent to one *million* tons of TNT or 10^3 kt] is released in the conversion of 46.58 grams of mass; and the largest thermonuclear device [bomb] ever detonated, about 100 megatons' worth, converted some 4.658 kg of mass directly into raw energy.

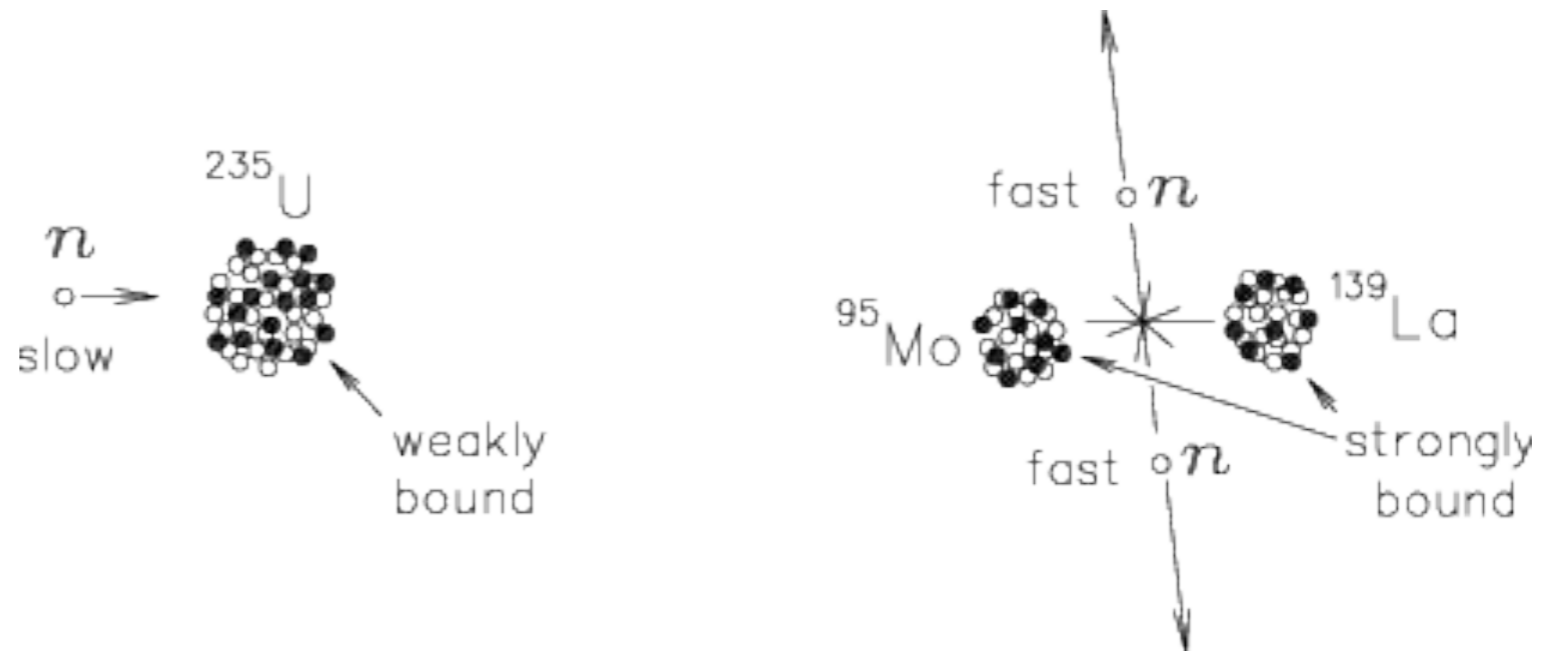
Nuclear Fission

Where did the energy come from? *What* mass got converted? To answer this question we must look at the processes involved on a sub-microscopic scale. First we must consider the natural tendency for oversized atomic nuclei to spontaneously *split* into smaller components. This process is known as NUCLEAR FISSION and is the energy source for all presently functioning NUCLEAR REACTORS on Earth. [Also for so-called "atomic" bombs.]

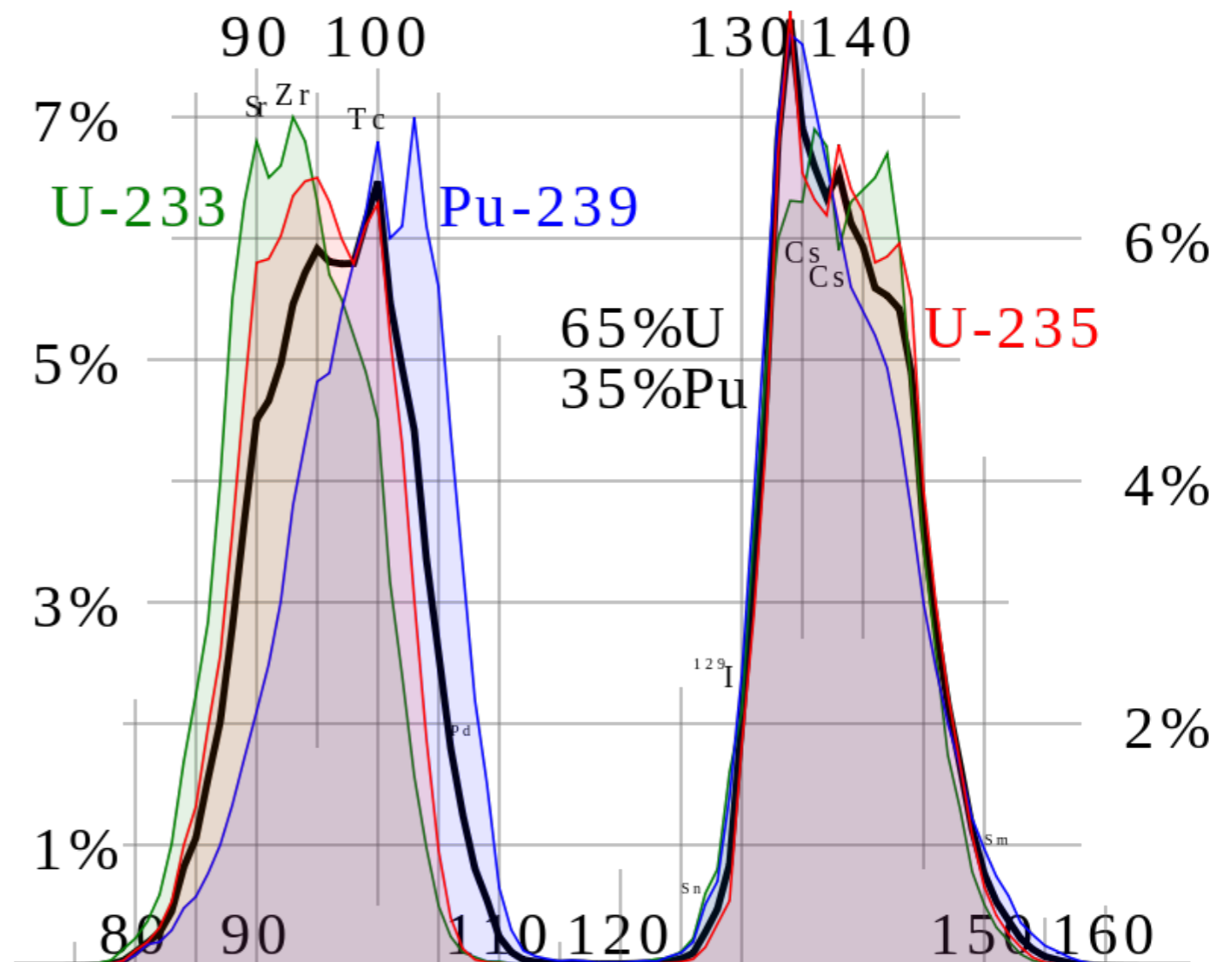


Fission of ^{235}U : The net mass of the initial neutron plus the ^{235}U nucleus is $219,883 \text{ MeV}/c^2$. The net mass of the fission products (two neutrons, a ^{95}Mo nucleus and a ^{139}La nucleus) is $219,675 \text{ MeV}/c^2$ - smaller because of the stronger *binding* of the Mo and La nuclei. The "missing mass" of $208 \text{ MeV}/c^2$ (a little less than 0.1% of the original mass) goes into the *kinetic energy* of the *fragments* (mainly the *neutrons*), which of course adds up to 208 MeV.

FISSION



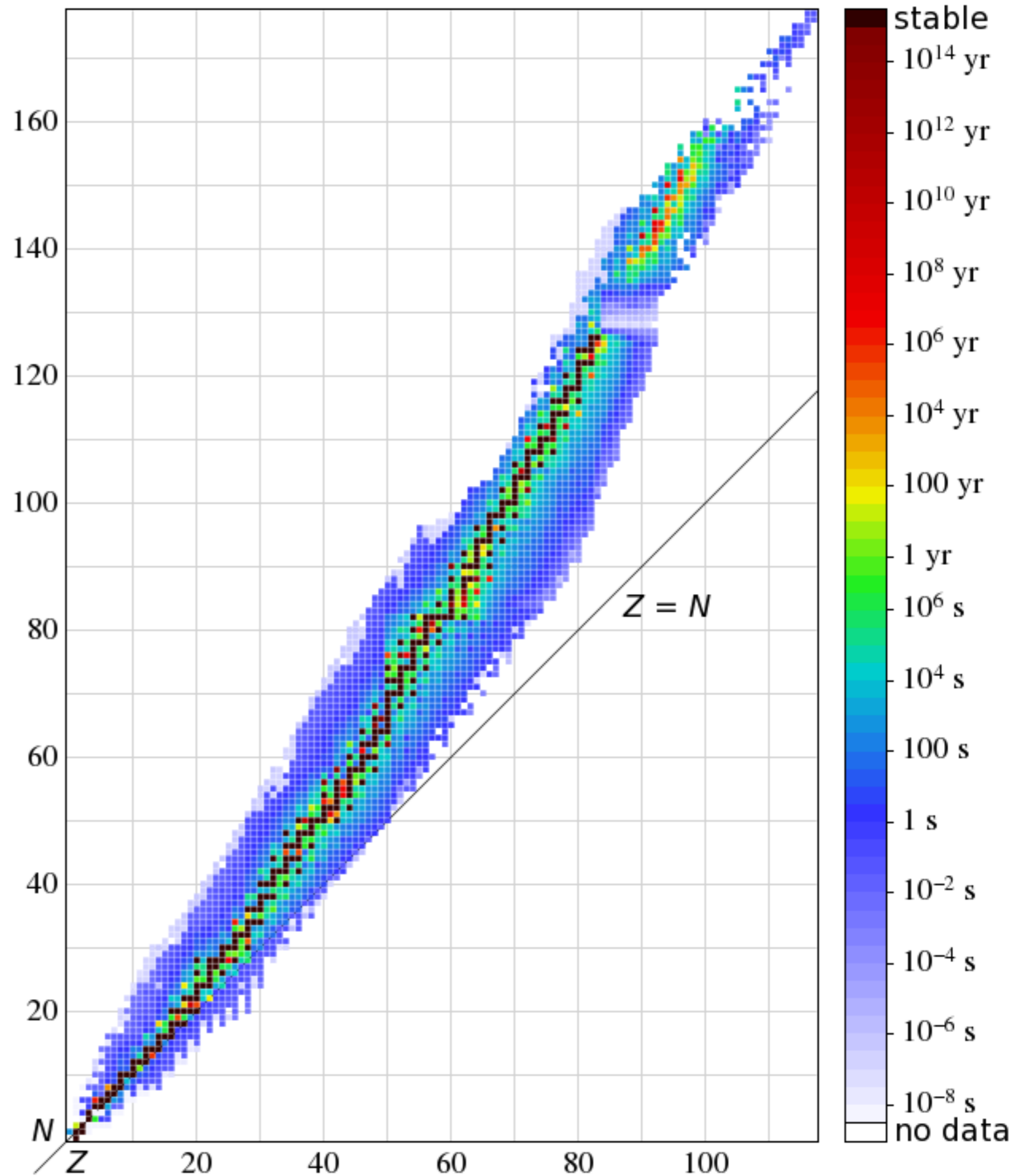
The example shown above has ^{235}U splitting into ^{95}Mo and ^{139}La along with *two* fast neutrons, but there are *many other ways* that ^{235}U can fission. One of its "daughters" usually has 90-100 nucleons, while the other has 130-140. And sometimes there are more than two neutrons emitted. This, plus the long lifetime of ^{235}U and its relatively innocuous alpha-decay, make it a "good" candidate for a **bomb**.



ISOTOPES and their (color-coded) Half-Lives

Z = # of protons

N = # of neutrons

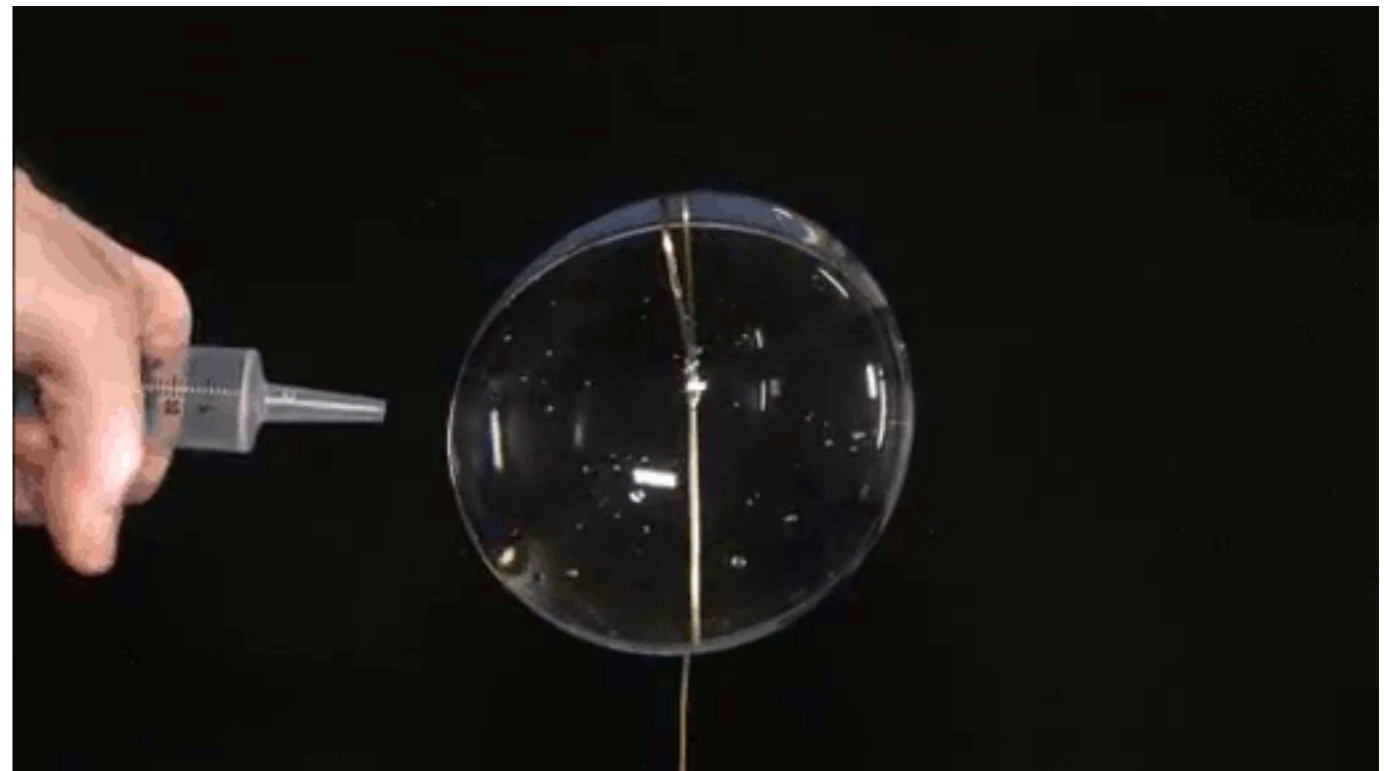


Liquid Drop Model



Surface tension keeps *small* water droplets perfectly spherical, but **big** water droplets are *unstable* because the attractive force between molecules is *short-range*.

Nuclei are similar: *small* ones are *stable*, but **big** ones jiggle and sometimes *split* into smaller nuclei, spitting out neutrons, for the same reason: the **strong attraction** between nucleons is *short* range, while the electrostatic *repulsion* between *protons* is *long* range.

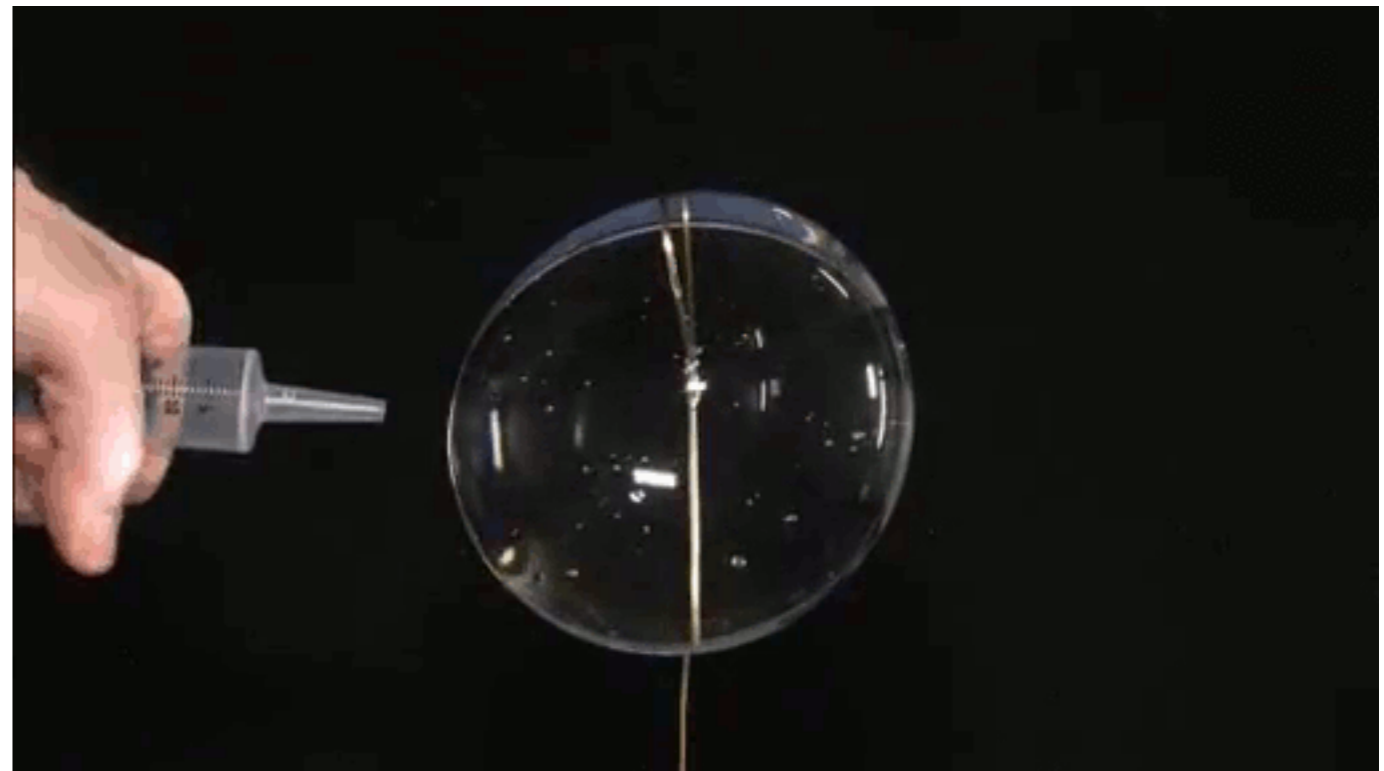


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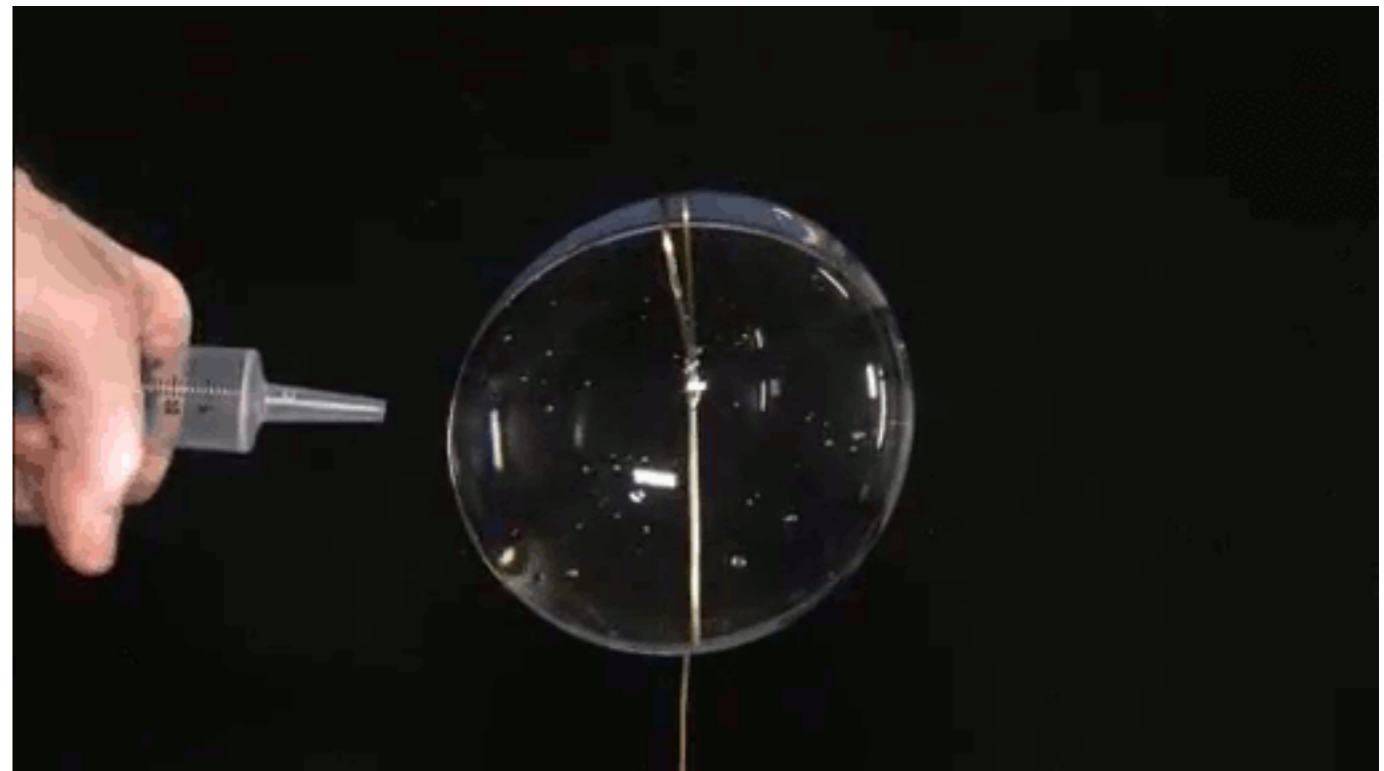


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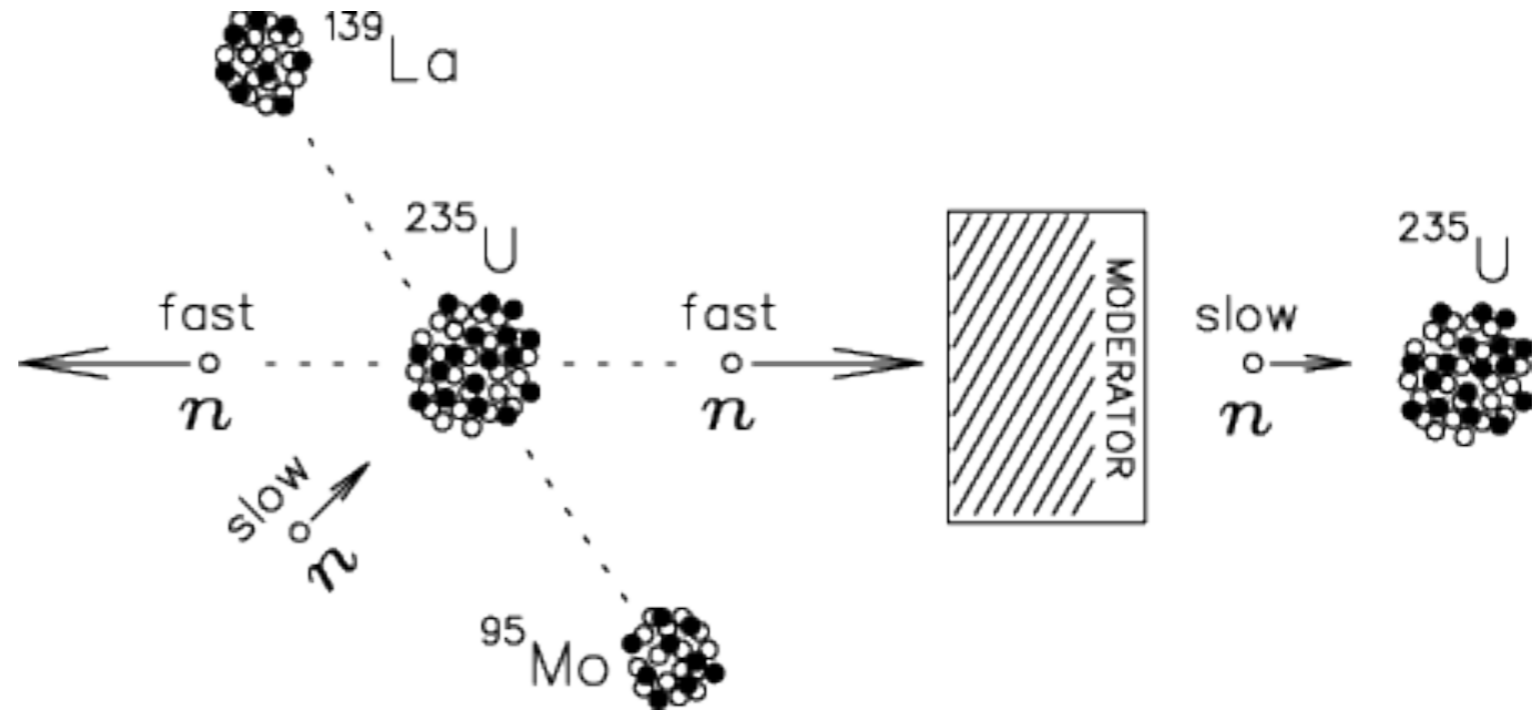


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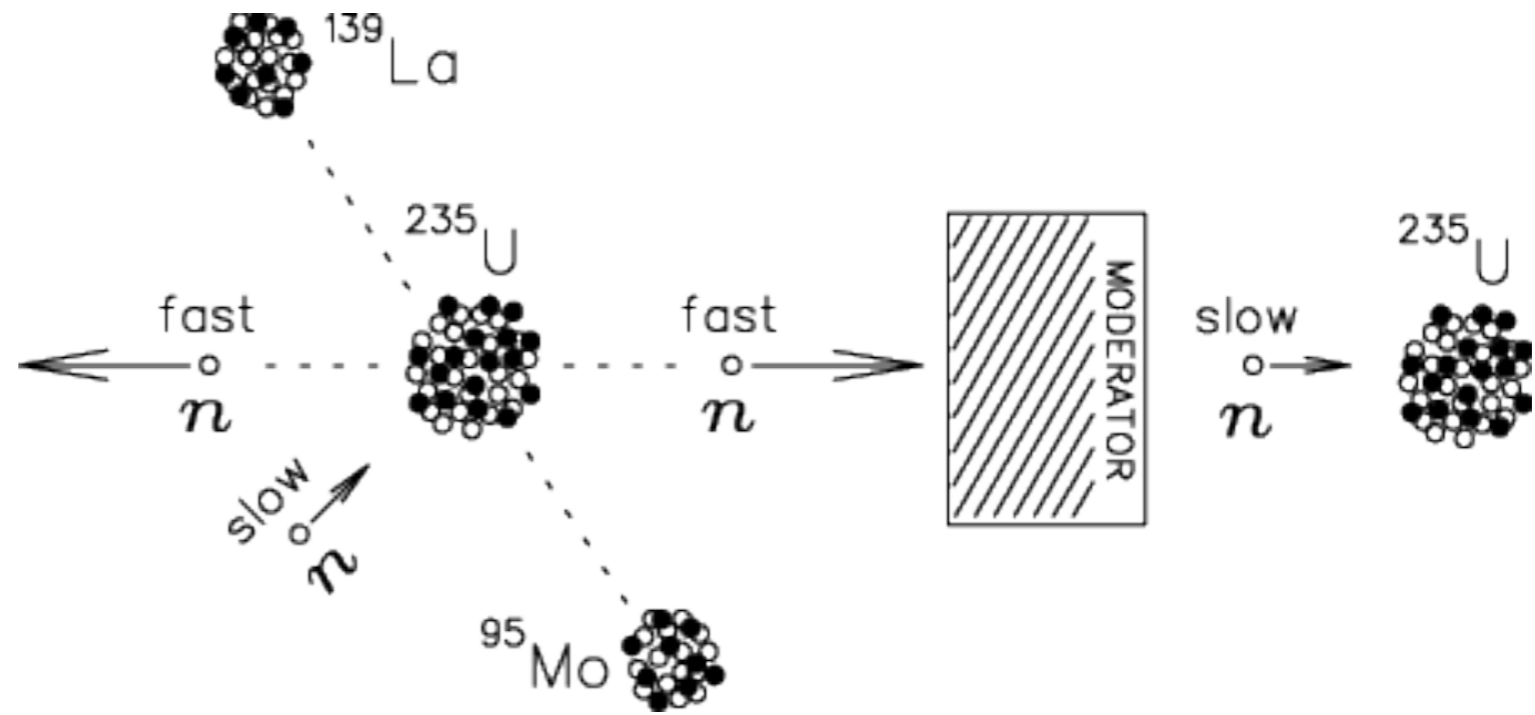


Chain Reactions:



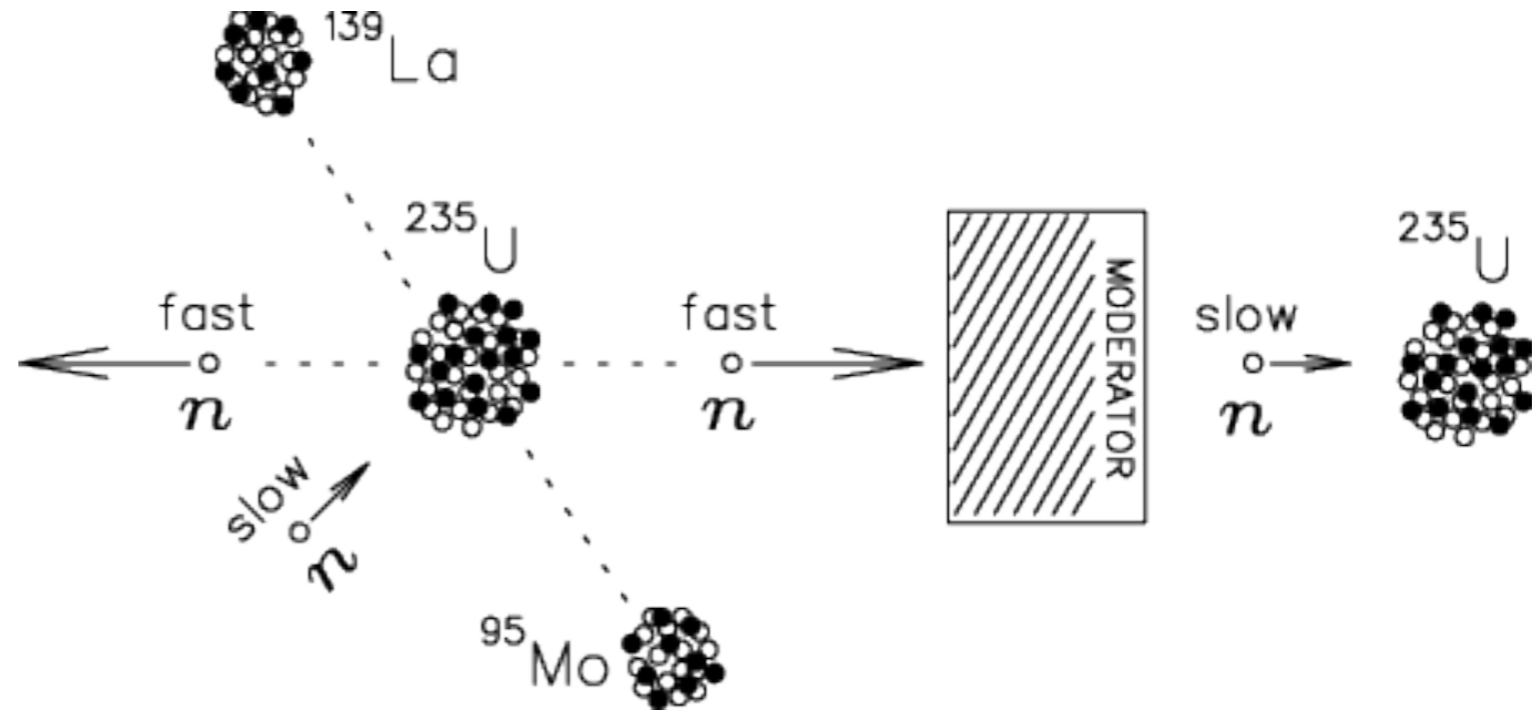
Chain Reactions:

- ^{235}U by itself:

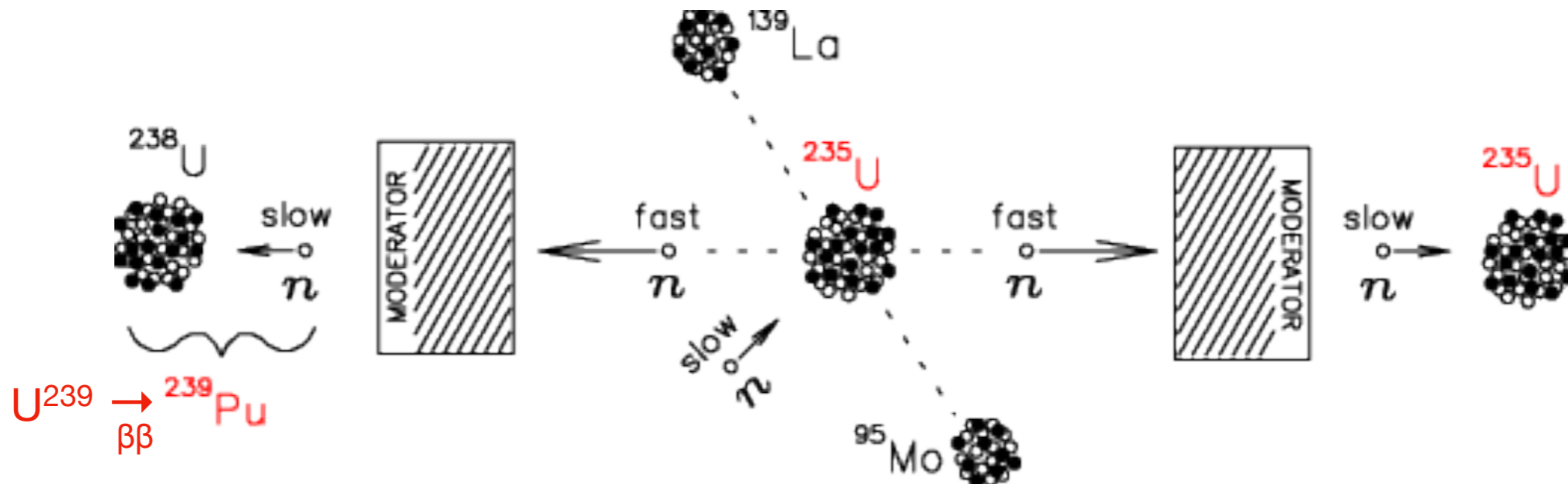


Chain Reactions:

- ^{235}U by itself:



- Breeding *fissile* ^{239}Pu from *fertile* ^{238}U with *neutrons* from ^{235}U :



How (e.g.) ^{235}U Bombs Work

1. Sub-critical chunks of ^{235}U are blasted together by conventional explosives, producing a temporary blob of *extremely* compressed ^{235}U .
2. A stray neutron is captured by ^{235}U , causing it to fission into two lighter nuclei and *several* neutrons.
3. Those neutrons slow down in the hyperdense metal and capture on other ^{235}U nuclei, causing *them* to fission...

CHAIN REACTION!

How *(some)* “H-Bombs” Work

1. Set off a small (*e.g.*) ^{235}U **fission** bomb to produce extreme pressure and temperature.
2. This triggers the **fusion** of (*e.g.*) deuterium & tritium, releasing huge amounts of energy, mainly in the form of *fast neutrons*.
3. *Fast* neutrons hit surrounding ^{238}U nuclei, causing *them* to **fission**...
4. Add as much ^{238}U as you like. It's a **fission** bomb!

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- Establish a *controlled* chain reaction in fission “fuel” using a combination of **moderators** (to slow down the fast fission neutrons so they can be captured and cause additional fissions) and neutron-absorbing “**control rods**” to decrease the slow neutron flux.

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- **Heat** results from the energy deposited. Use it to drive a thermodynamic **heat engine** (e.g. a steam turbine). The hotter, the higher the efficiency.

$$(\text{Carnot efficiency} = 1 - T_{\text{cold}}/T_{\text{hot}})$$

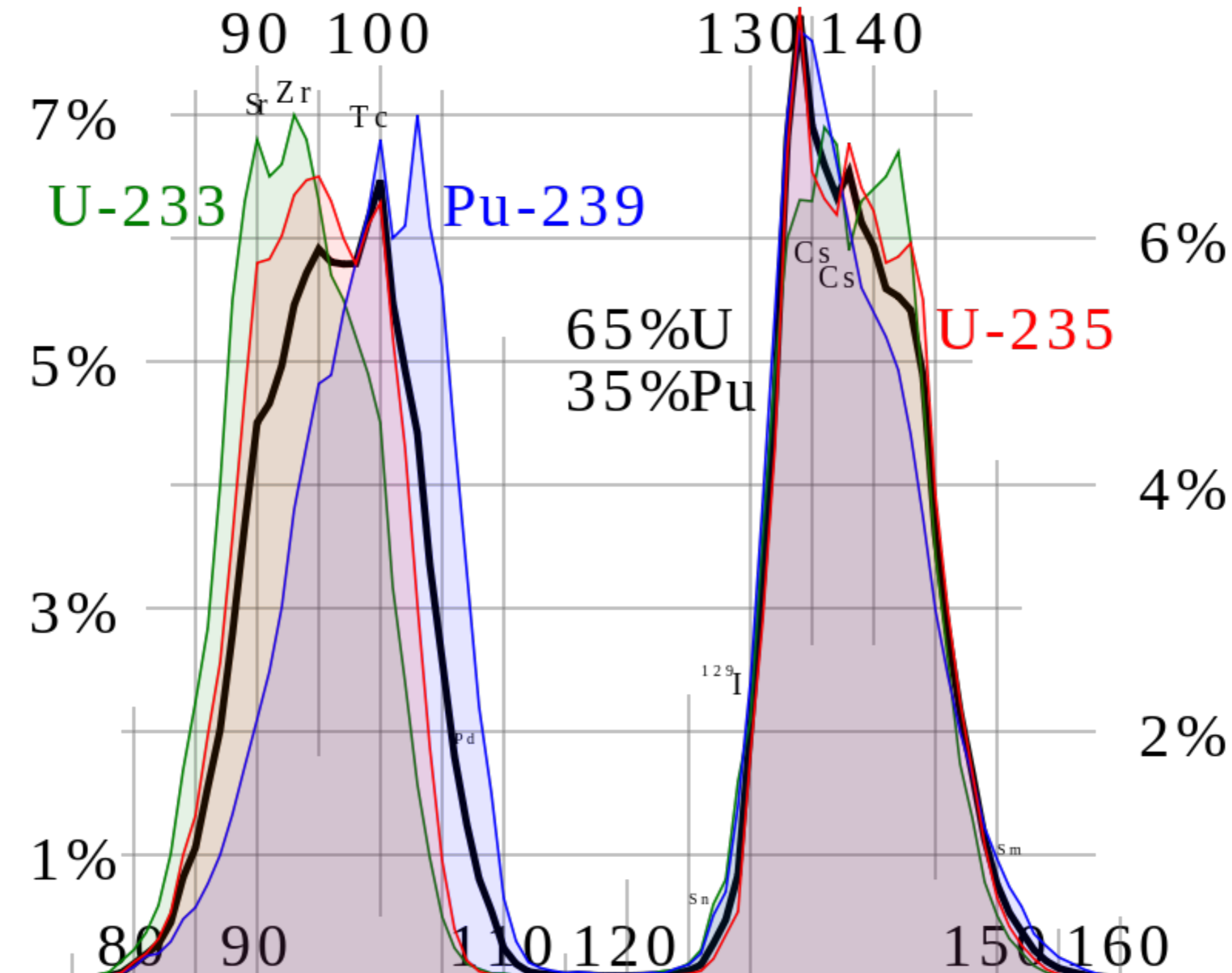
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- That’s it. There are almost no exceptions *so far*.

Fission Products



Decay of Fission Products

Wikipedia: “The radioactivity in the fission product mixture is [initially] mostly *short-lived* isotopes such as ^{131}I and ^{140}Ba ; after about four months ^{141}Ce , $^{95}\text{Zr}/^{95}\text{Nb}$ and ^{89}Sr take the largest share, while after about two or three years the largest share is taken by $^{144}\text{Ce}/^{144}\text{Pr}$, $^{106}\text{Ru}/^{106}\text{Rh}$ and ^{147}Pm .”

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Medium-lived Daughters

Prop:	$t_{1/2}$	Yield	Q^*	$\beta\gamma^*$
Unit:	(a)	(%)	(keV)	
^{155}Eu	4.76	0.0803	252	$\beta\gamma$
^{85}Kr	10.76	0.2180	687	$\beta\gamma$
$^{113\text{m}}\text{Cd}$	14.1	0.0008	316	β
^{90}Sr	28.9	4.505	2826	β
^{137}Cs	30.23	6.337	1176	$\beta\gamma$
$^{121\text{m}}\text{Sn}$	43.9	0.00005	390	$\beta\gamma$
^{151}Sm	88.8	0.5314	77	β

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Long-lived Daughters

Nuclide	$t_{1/2}$	Yield	Decay energy ^[a 1]	Decay mode
	(Ma)	(%) ^[a 2]	(keV)	
^{99}Tc	0.211	6.1385	294	β
^{126}Sn	0.230	0.1084	4050 ^[a 3]	$\beta\gamma$
^{79}Se	0.327	0.0447	151	β
^{93}Zr	1.53	5.4575	91	$\beta\gamma$
^{135}Cs	2.3	6.9110 ^[a 4]	269	β
^{107}Pd	6.5	1.2499	33	β
^{129}I	15.7	0.8410	194	$\beta\gamma$

Health Concerns

Isotope	Radiation	Half-life	GI absorption	Notes
Strontium-90/yttrium-90	β	28 years	30%	
Caesium-137	β, γ	30 years	100%	
Promethium-147	β	2.6 years	0.01%	
Cerium-144	β, γ	285 days	0.01%	
Ruthenium-106/rhodium-106	β, γ	1.0 years	0.03%	
Zirconium-95	β, γ	65 days	0.01%	
Strontium-89	β	51 days	30%	
Ruthenium-103	β, γ	39.7 days	0.03%	
Niobium-95	β, γ	35 days	0.01%	
Cerium-141	β, γ	33 days	0.01%	
Barium-140/lanthanum-140	β, γ	12.8 days	5%	
Iodine-131	β, γ	8.05 days	100%	
Tritium	β	12.3 years	100%	[a]